Stat 344 - Fall 2024

Homework Assignment 6

Due: Tuesday, December 10th on Learning Suite at 2:00 pm

1. A person age x purchases a fully discrete 3-year term insurance. The death benefit for the policy is \$100,000 plus the sum of all premiums paid. Use the following basis for all calculations:

 $q_x = 0.1, \qquad q_{x+1} = 0.2, \qquad q_{x+2} = 0.3, \qquad i = 10\%$

- (a) Calculate the net annual premium. [26135.78]
- (b) Write a prospective formula for ${}_{1}V^{n}$ in terms of insurance and annuity symbols. Use this equation to calculate ${}_{1}V^{n}$. [17928.7]
- (c) Write an equation for ${}_{2}V^{n}$ in terms of ${}_{1}V^{n}$. Use this equation to solve for ${}_{2}V^{n}$.
- (d) Write an equation for ${}_{2}V^{n}$ in terms of ${}_{3}V^{n}$. Use this equation to solve for ${}_{2}V^{n}$.
- 2. A single premium continuous whole life annuity is issued to (65). The annuity pays at a rate of \$5,000 per year. The premium and policy value bases are:
 - Mortality is modeled as a constant force of mortality, $\mu = 0.07$.
 - Interest is given by $\delta = 0.03$.
 - The only expenses are an amount of \$1,000 incurred at policy issue and amount of \$500 incurred at the policy termination.
 - (a) Calculate the gross single premium for this policy. [51,350]
 - (b) Calculate the gross premium policy value at time 5 for this policy. [50,350]
- 3. A fully discrete whole life policy is issued to (45) whose death benefit is \$100,000 until the insured reaches age 65, and \$50,000 thereafter. Premiums are level and paid anually. Use the following basis for all calculations:
 - Mortality follows the SULT.
 - i = 5%
 - Expenses are:
 - -5% of all gross premiums
 - \$1,000 at the start of year 1; \$100 at the start of each subsequent year the policy is in force

- (a) Calculate the net and gross premiums for this policy. [492.60, 676.96]
- (b) Calculate ${}_{10}V^n$ and ${}_{10}V^g$ using prospective formulas. [5086.51, 4275.30]
- (c) Calculate $_{11}V^n$ and $_{11}V^g$ using recursion formulas. [5670.07, 4869.74]
- 4. A single premium whole life annuity-due is issued to (65) that pays a monthly benefit of \$1,000. The first 10 years of payments are guaranteed. The only expenses are \$700 at issue and \$45 per year in renewal years. (Assume that the renewal expenses are incurred only while the policyholder is alive.) Assume that mortality is given by the SULT; use the UDD fractional age assumption where necessary. Also assume an annual effective interest rate of 5%.
 - (a) Calculate the net single premium for this policy. [160,546.62]
 - (b) Calculate the gross single premium for this policy. [161,811.40]
 - (c) Calculate ${}_{8}V^{n}$, ${}_{8}V^{g}$, and ${}_{8}V^{e}$ for this policy, assuming the insured is alive at that time. [126,850.76; 127,346.10; 495.36]
 - (d) Calculate ${}_{12}V^n$ for this policy. [109,798.95]
 - (e) Calculate $_{0.05}p_{76.95}$ for this person. [0.998946]
 - (f) Calculate $_{11.95}V^n$ for this policy. [109,415.96]
- 5. Jill purchases a \$250,000 fully discrete 20-year term life insurance policy at age 35. Mortality is given by the SULT. Assume an annual effective interest rate of 5%. Expenses are as follows:
 - Issue expenses of \$1,000.
 - Maintenance expenses of \$50 per year in renewal years.
 - Premium taxes of 2% of all gross premiums.
 - Claims expenses of \$100 at the end of the year of death.
 - (a) Calculate ${}_{5}V^{n}$, ${}_{5}V^{g}$, and ${}_{5}V^{e}$ for this policy. [444.02, -347.06, -791.08]
 - (b) Calculate the FPT modified premiums for this policy. [93.10, 187.63]
 - (c) Calculate ${}_{5}V^{FPT}$ for this policy. [366.02]